

# Model-independent constraints in the context of multi-messenger cosmology

CosmoVerse@Istanbul - June 25 - Istanbul

**Andrea Cozzumbo**

Riccardo Murgia Gor Oganesyan Marica Branchesi



**JCAP05(2025)021**



**Andrea Cozzumbo**

[andrea.cozzumbo@gssi.it](mailto:andrea.cozzumbo@gssi.it)

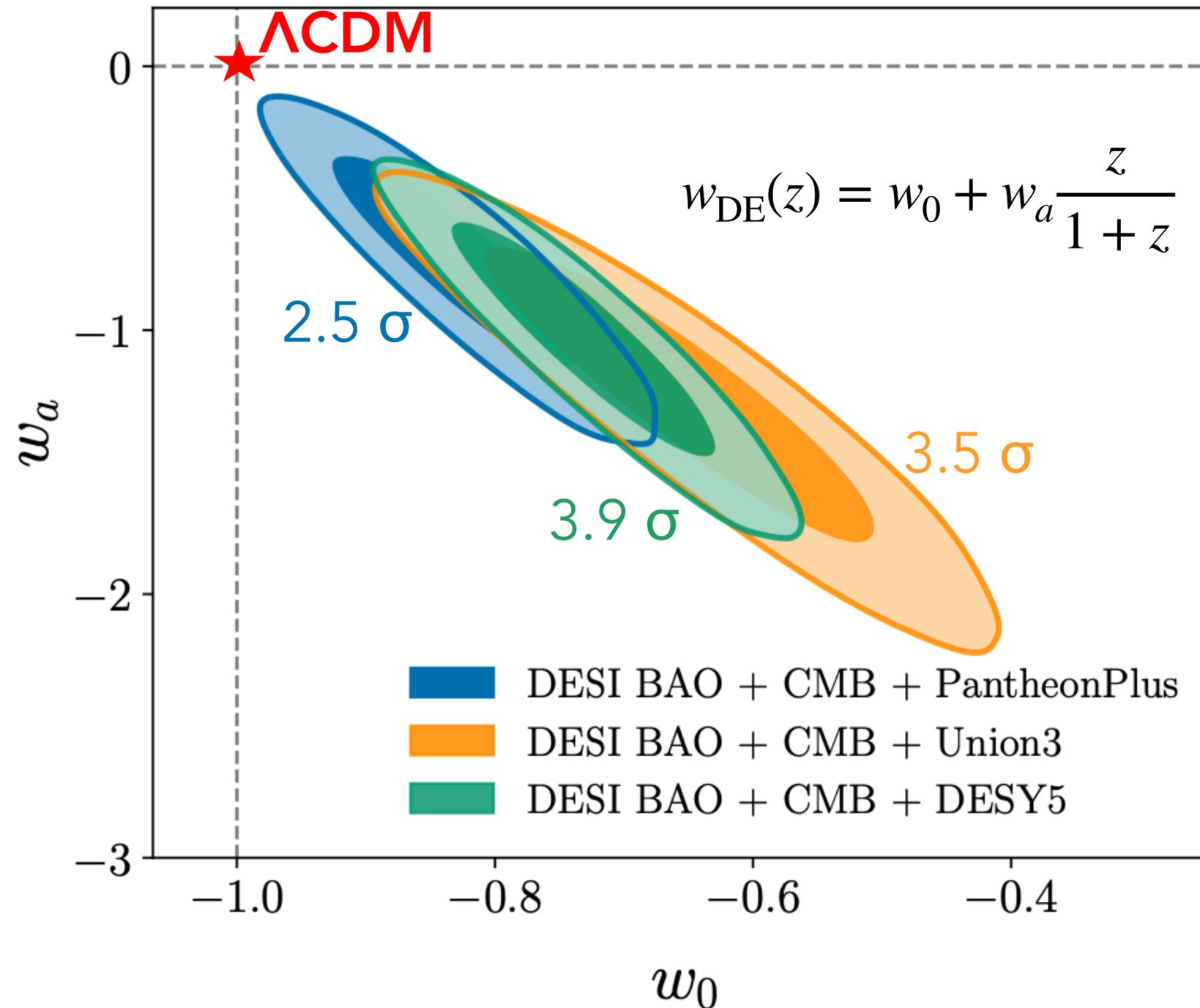
in collaboration with

**Ulyana Dupletsa   Rodrigo Calderón   Riccardo Murgia**

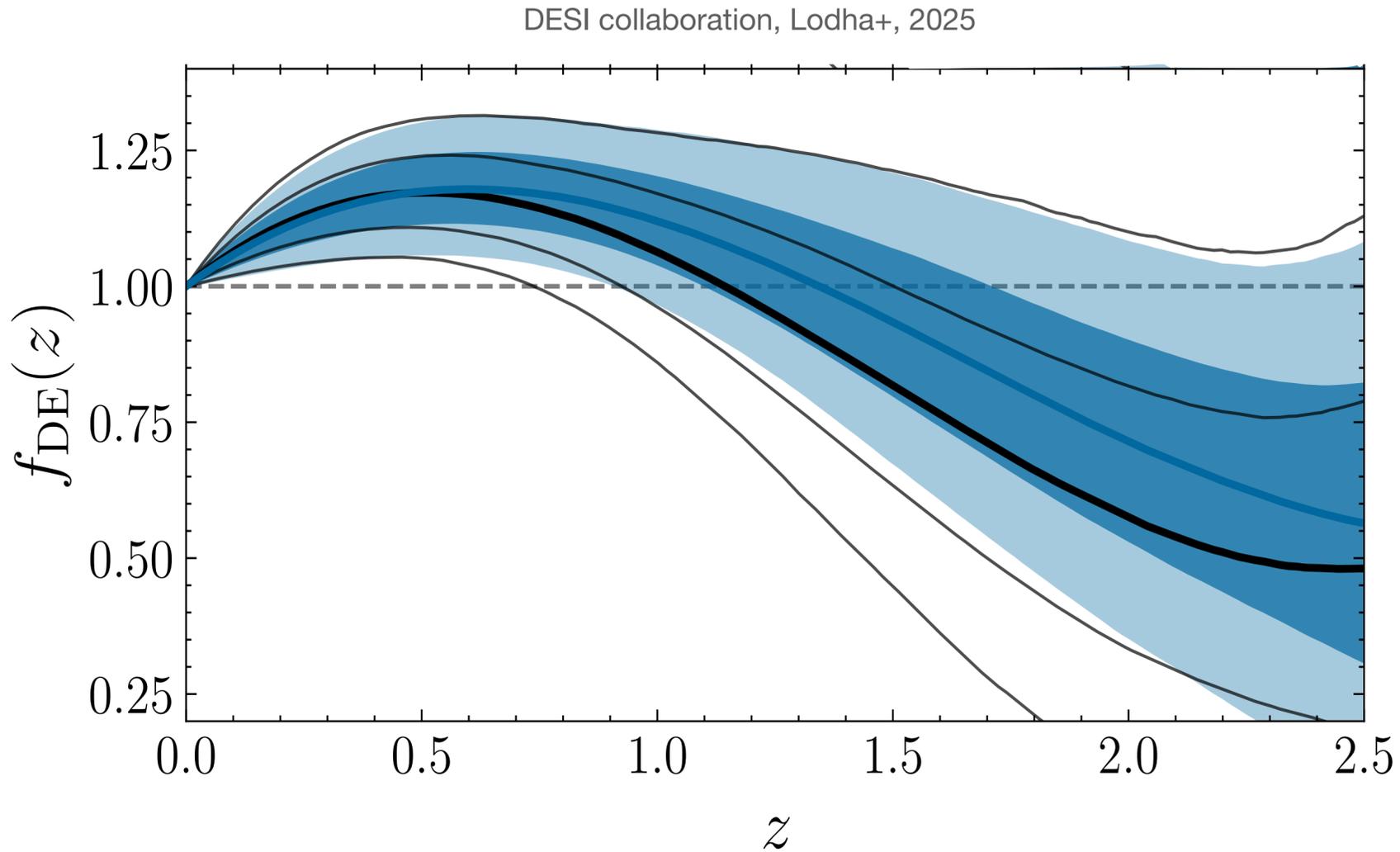
**Gor Oganesyan   Marica Branchesi**

# “Tantalizing suggestion” of dynamical DE

DESI collaboration, Adame+, 2024



# “Tantalizing suggestion” of dynamical DE



$$H(z) = H_0 \sqrt{\Omega_{m,0}(1+z)^3 + \Omega_{\text{DE},0} \exp \left[ 3 \int_0^z \frac{1 + w_{\text{DE}}(z')}{1+z'} dz' \right]}$$

$$w_{\text{DE}}(z) = w_0 + w_a \frac{z}{1+z}$$

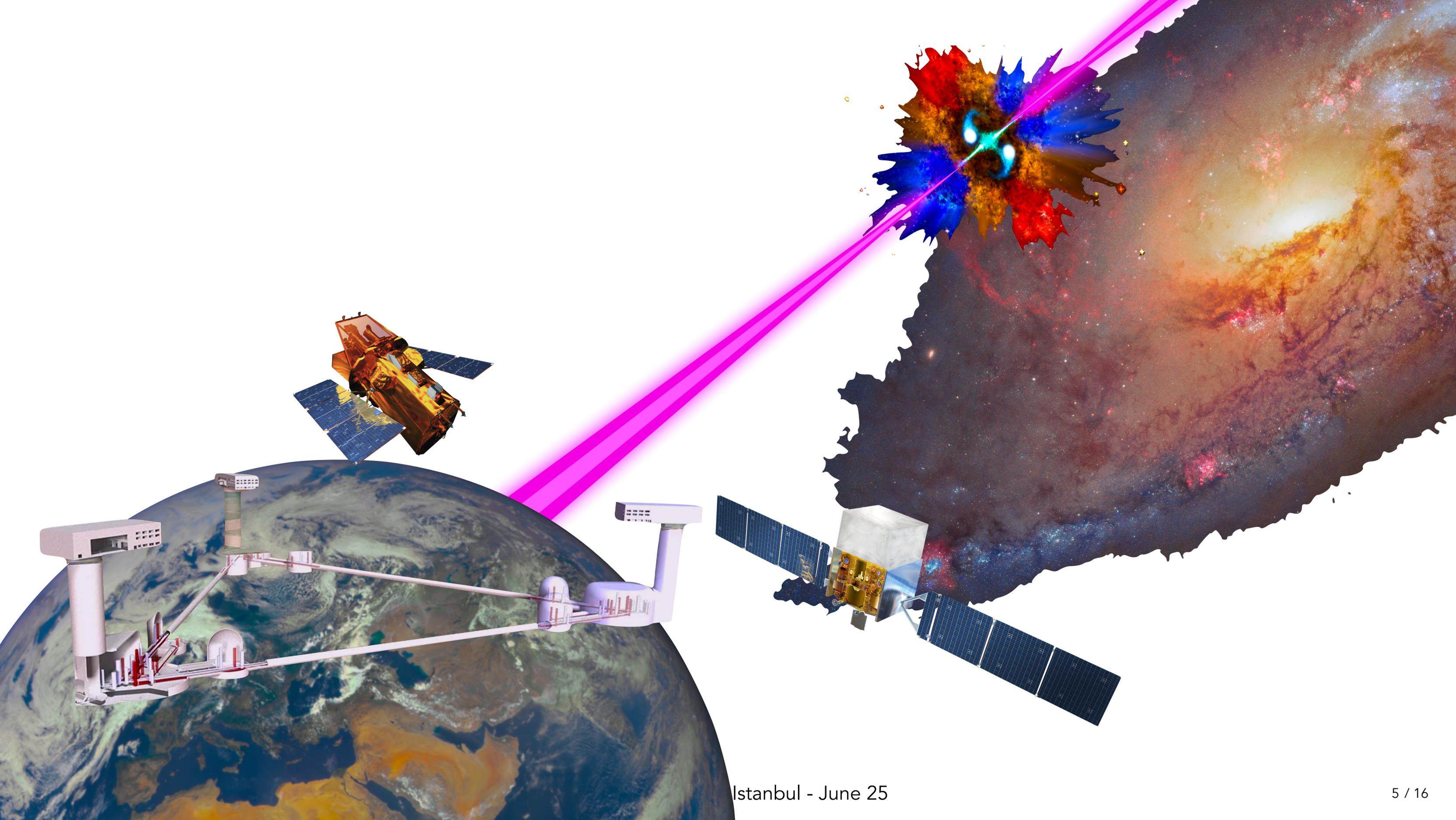
$$f_{\text{DE}}(z) = (1+z)^{3(1+w_0+w_a)} \exp \left[ \frac{-3w_a z}{1+z} \right]$$

# Why GWs

$$\tilde{h}_+(f) \propto \frac{\mathcal{M}^{5/6}}{2 d_L} f^{-7/6} e^{i\phi(\mathcal{M}, f)} (1 + \cos^2(\iota)) \quad \tilde{h}_\times(f) \propto \frac{\mathcal{M}^{5/6}}{d_L} f^{-7/6} e^{i\phi(\mathcal{M}, f) + i\pi/2} \cos(\iota)$$

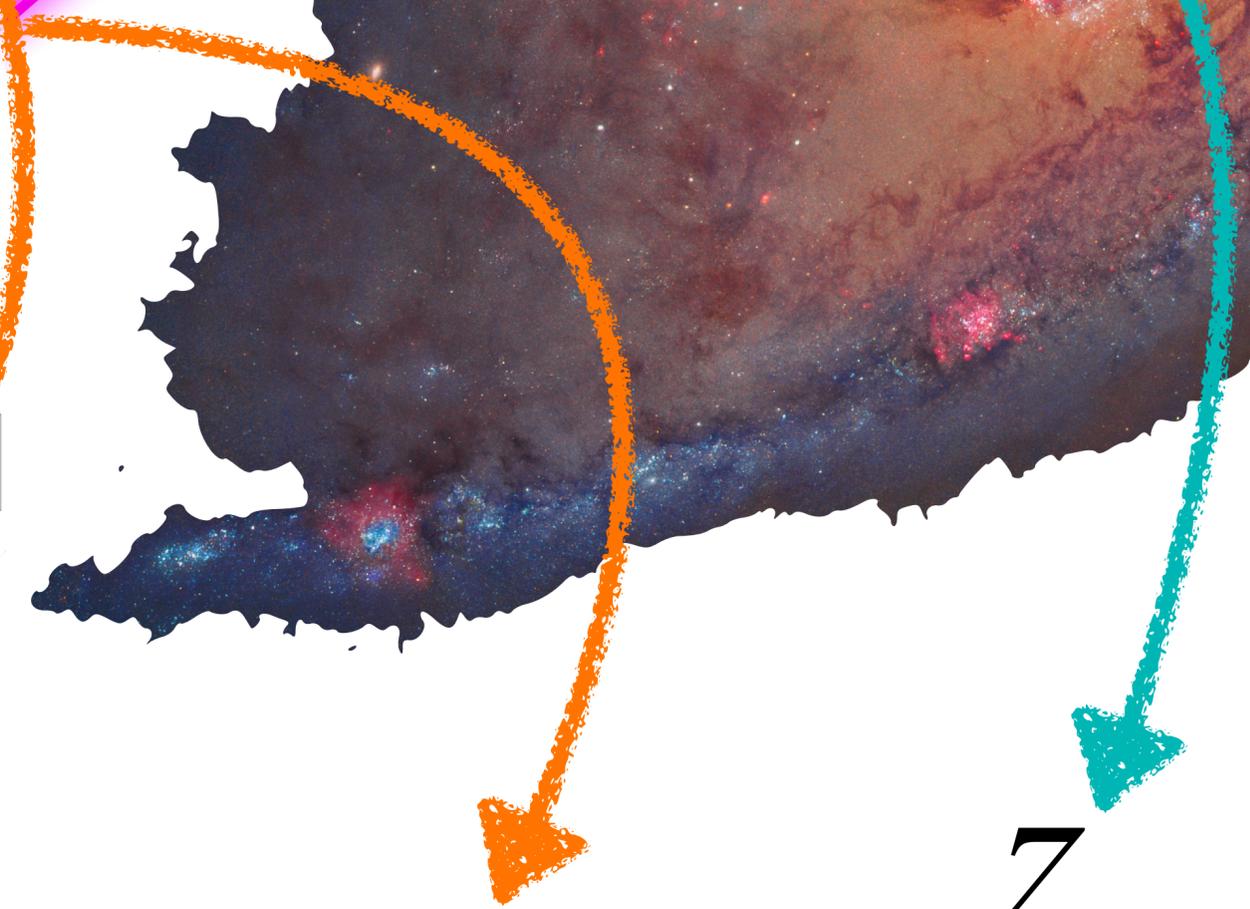
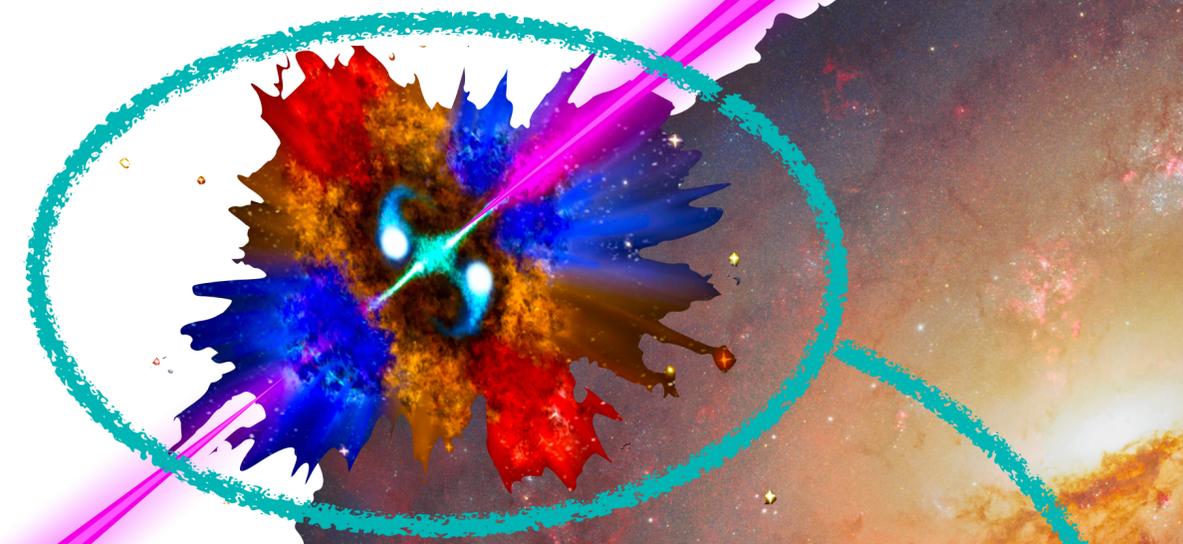
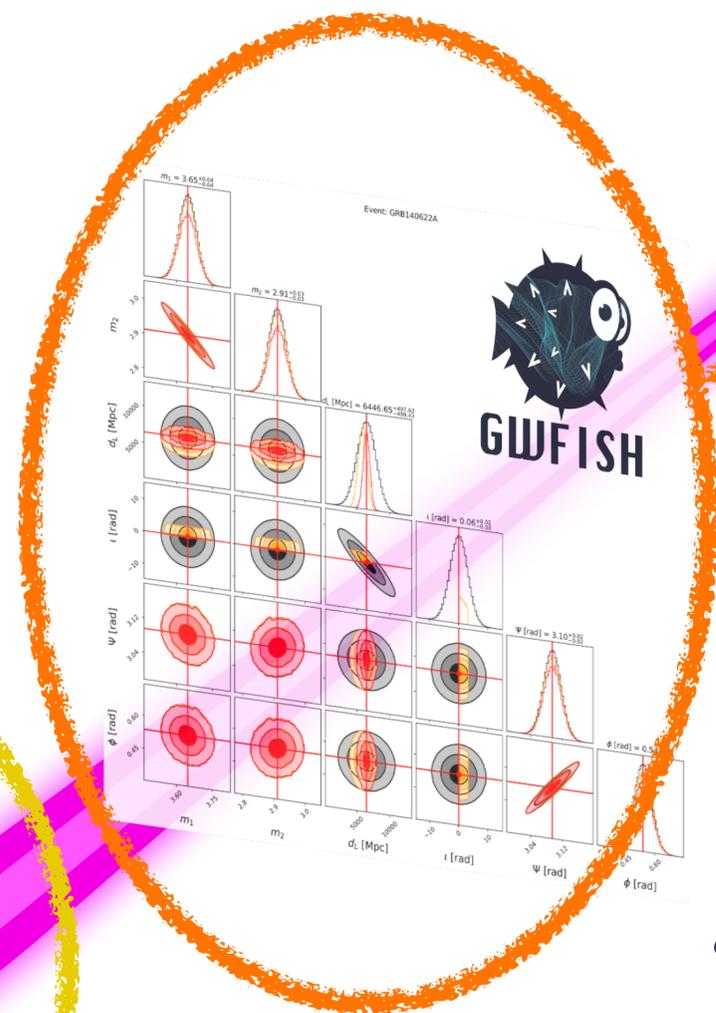
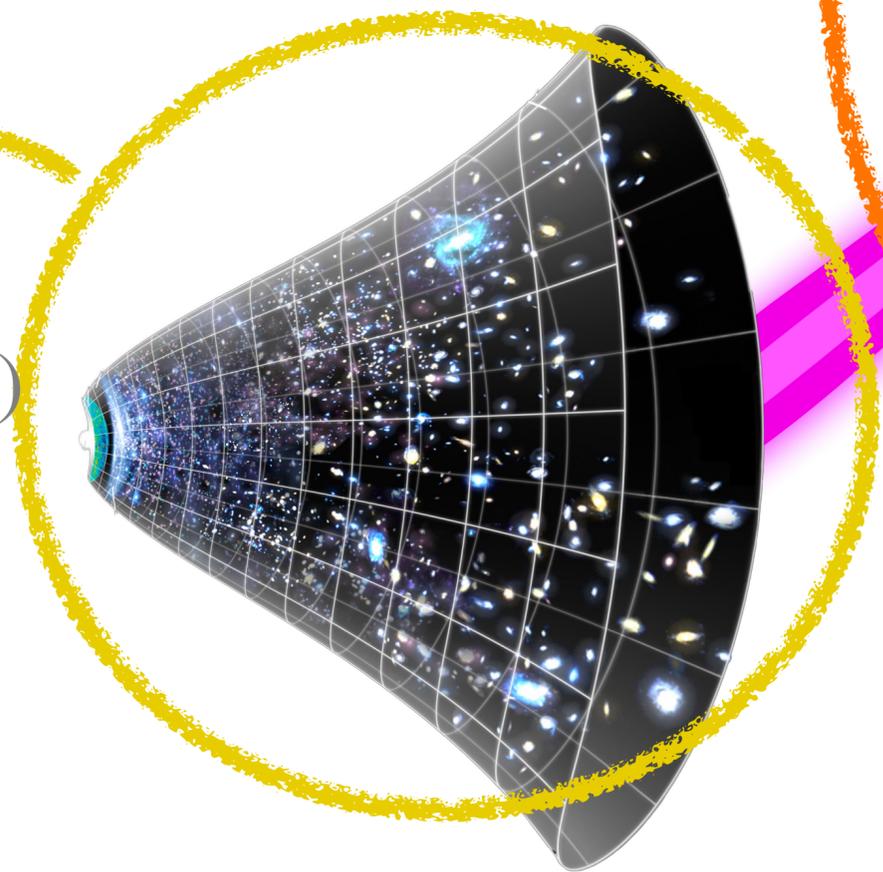
self-calibrated measure of distance

$$d_L(z) = c \left(1 + \overset{?}{z}\right) \int_0^z \frac{dz'}{H(z')}$$



$$GP \sim \mathcal{N}(\mu, k)$$

$$H(z)$$

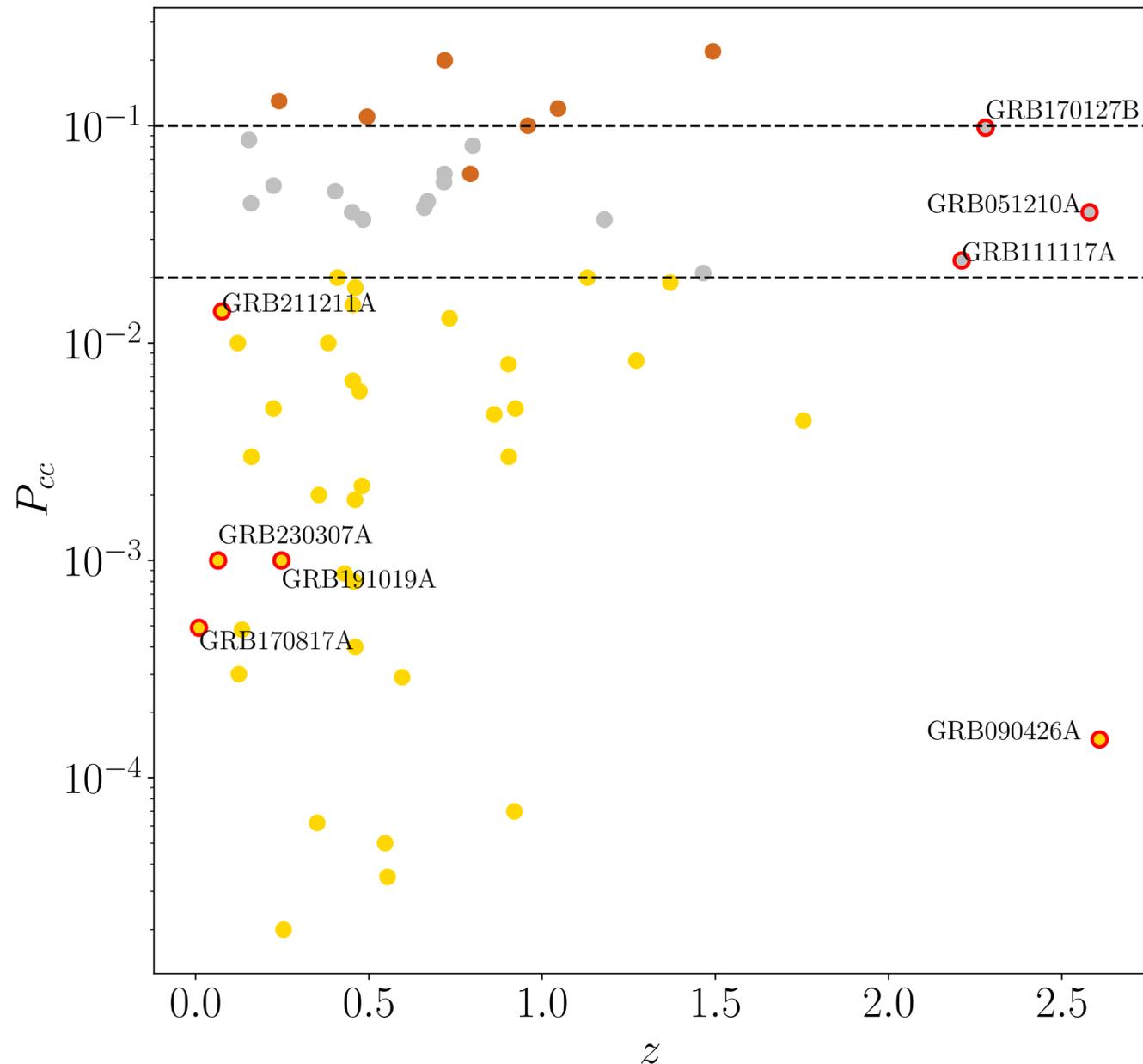


$$d_L(z)$$

$$z$$

# GRB data set

Cozzumbo+, 2024



- Fermi-GBM & Swift-BAT/UVOT/XRT
- Merger-driven GRB events
- $\Delta z \leq 7\%$

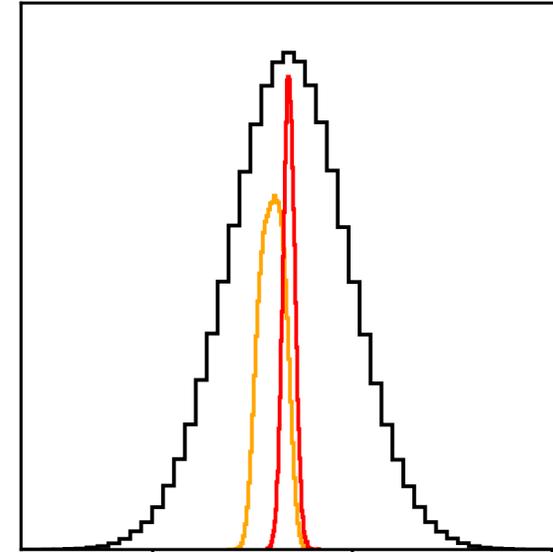
If **Einstein Telescope** existed during the **Swift** and **Fermi** era, what new insights into cosmology would we have today?

# GW posteriors

Duplesta+, 2024

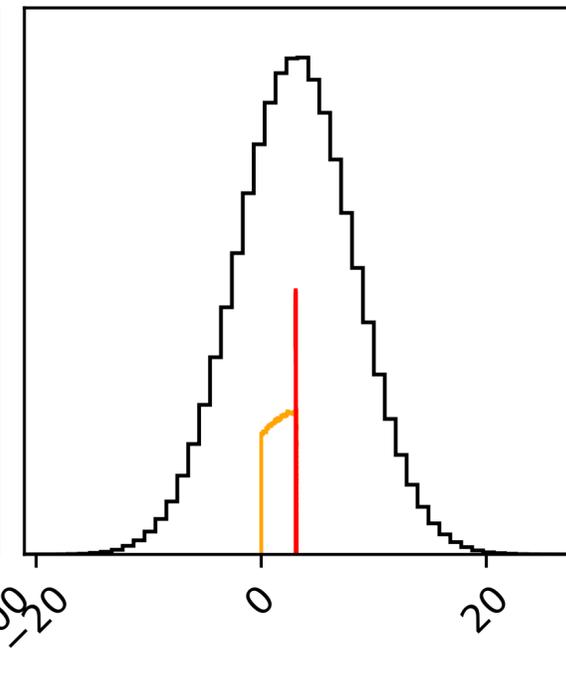
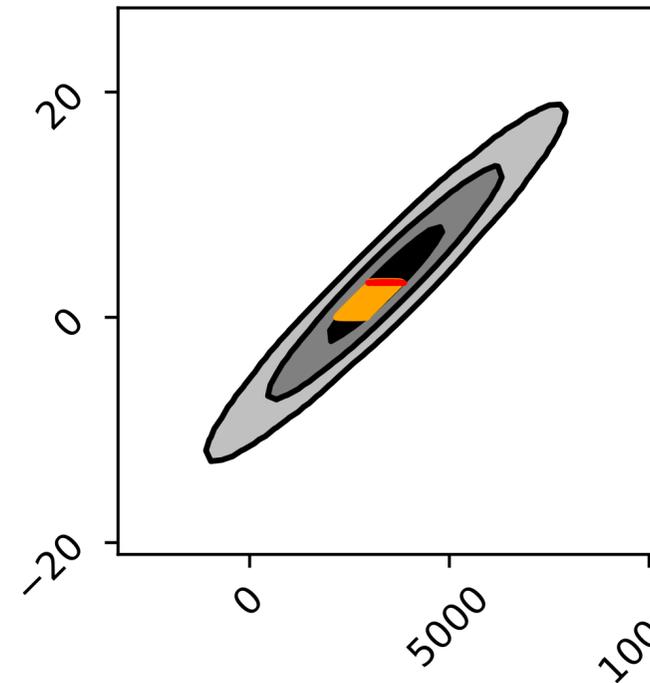


$$d_L \text{ [Mpc]} = 3411.56^{+148.72}_{-147.31}$$



@ fixed cosmology

$$\iota \text{ [rad]} = 3.08^{+0.03}_{-0.02}$$



$d_L$  [Mpc]

$\iota$  [rad]

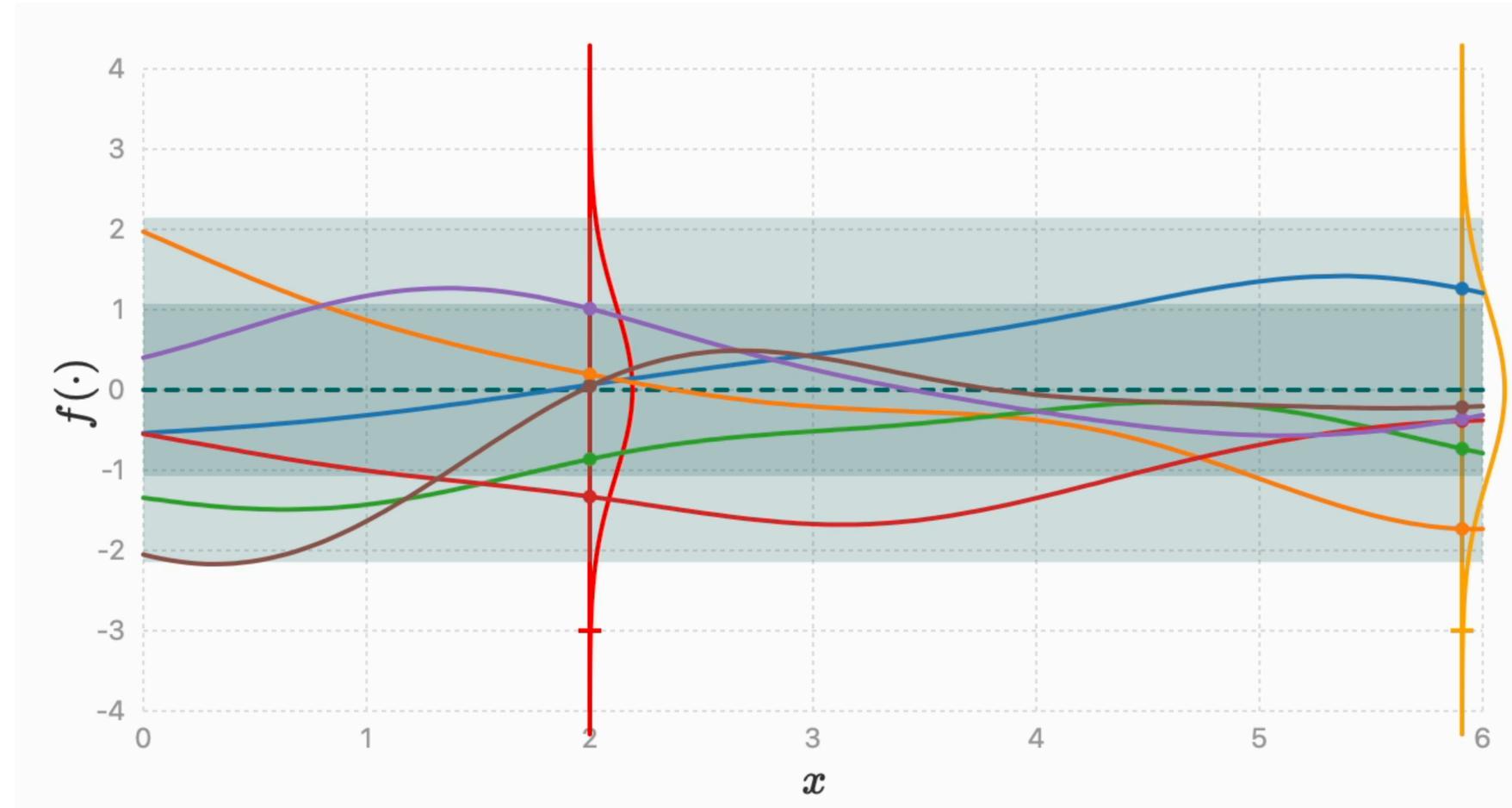
# Non-parametric approach

GP → Gaussian Process

$$h^2(z) = \frac{H^2(z)}{H_0^2} = \Omega_{m,0} (1+z)^3 + (1 - \Omega_{m,0}) f_{\text{DE}}(z)$$

$$f_{\text{DE}}(z) \sim GP(\bar{f}_{\text{DE}} = 1, k(\sigma_f, l_f))$$

$$k(\sigma_f, l_f) = \sigma_f^2 e^{-\frac{(x-x')^2}{2l_f^2}}$$



# Our strategy

- We generate mock joint GW-GRB data assuming 2 different cosmologies

$\Lambda$ CDM *Planck18*

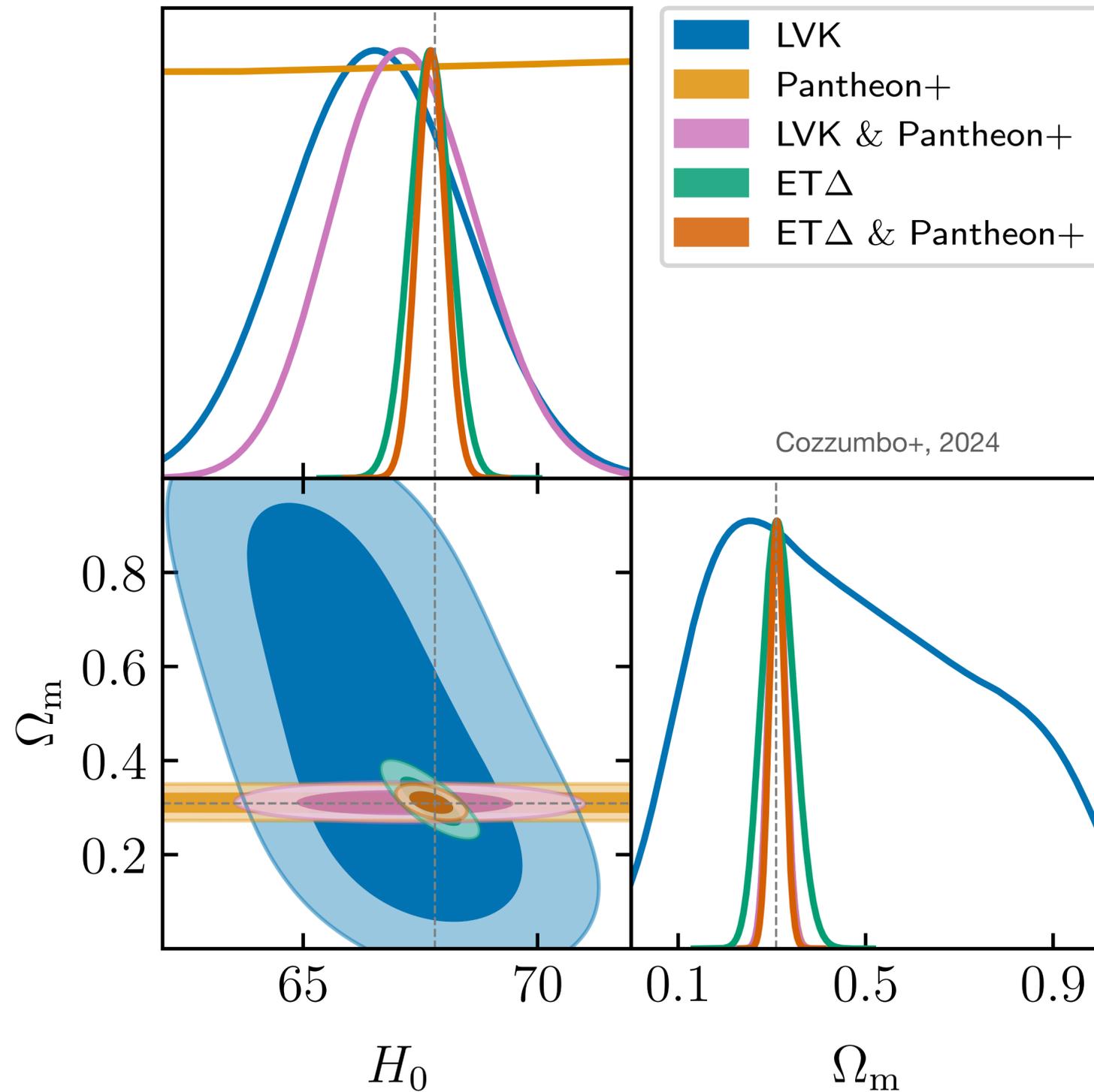
DDE *Planck18, eBOSS, Pantheon+*

- We fit them with a parametric and a non-parametric approach with various observational configurations
- We compare the performances

# Parametric approach

Injected

$\Lambda$ CDM *Planck18*



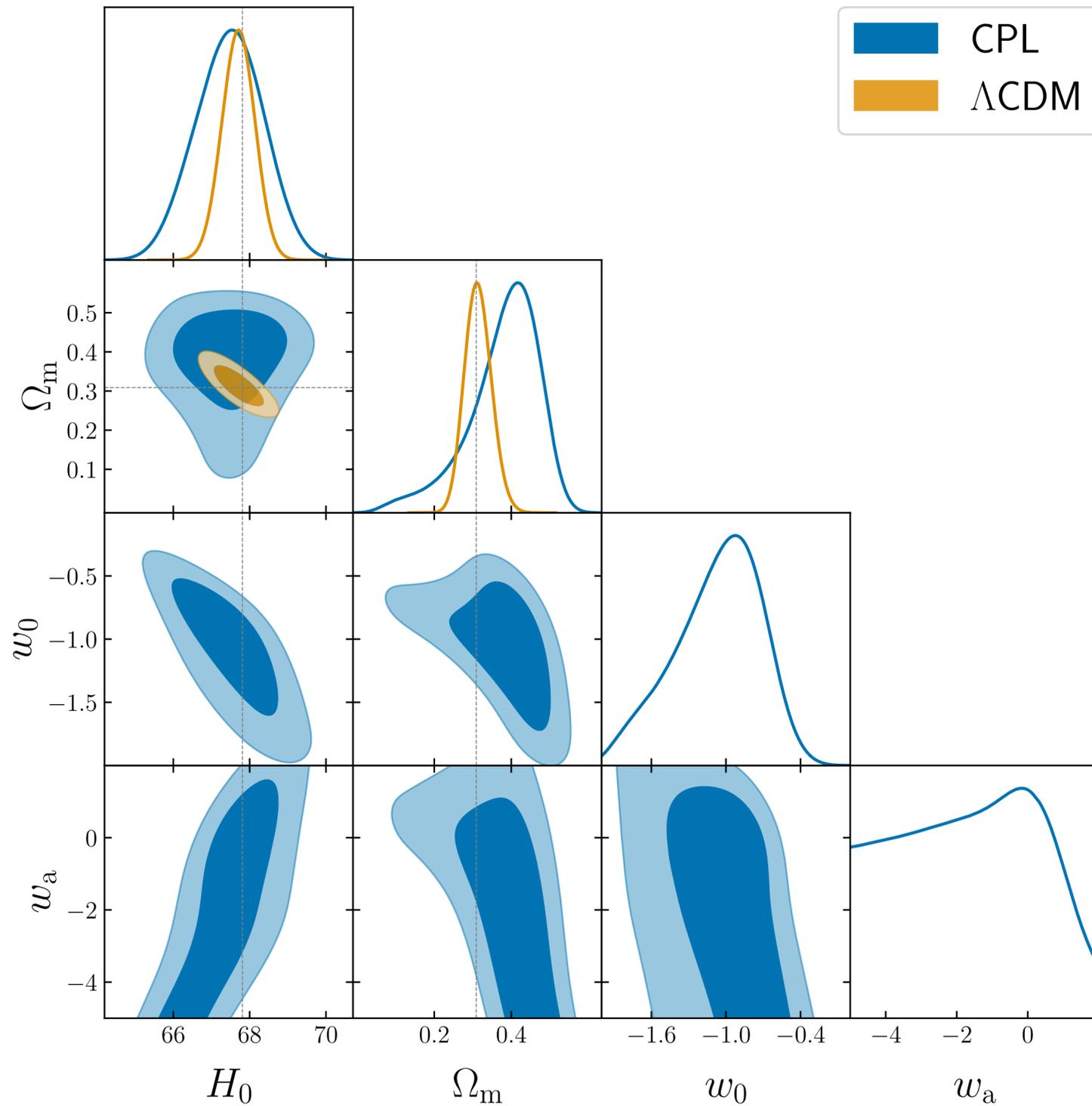
Fit

$\Lambda$ CDM

Injected

$\Lambda$ CDM Planck18

# Parametric approach



Fit  
CPL

$$h^2(z) = \frac{H^2(z)}{H_0^2} = \Omega_{m,0} (1+z)^3 + (1 - \Omega_{m,0}) f_{\text{DE}}(z)$$

$$w(z)^{\text{CPL}} = w_0 + w_a \frac{z}{1+z}$$

$$f_{\text{DE}}(z) = (1+z)^{3(1+w_0+w_a)} \exp\left[\frac{-3w_a z}{1+z}\right]$$

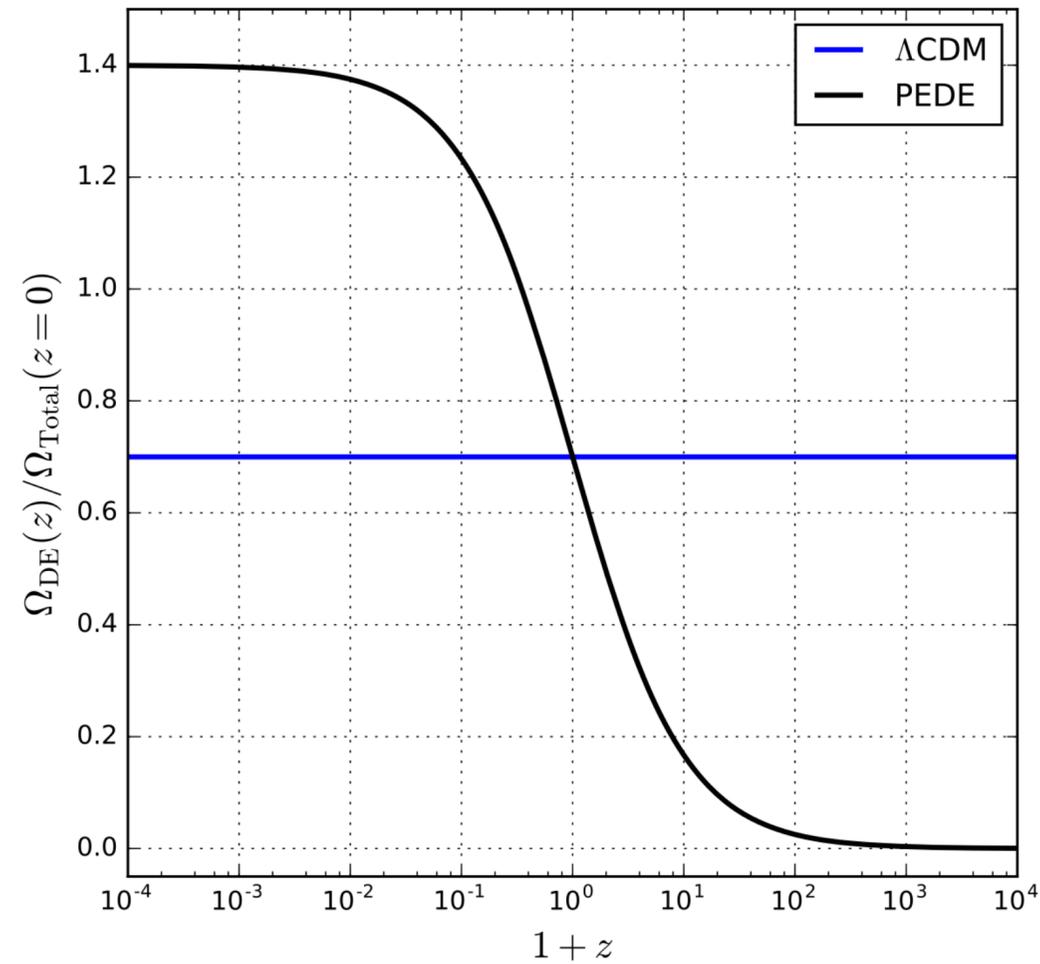
Cozzumbo+, 2024



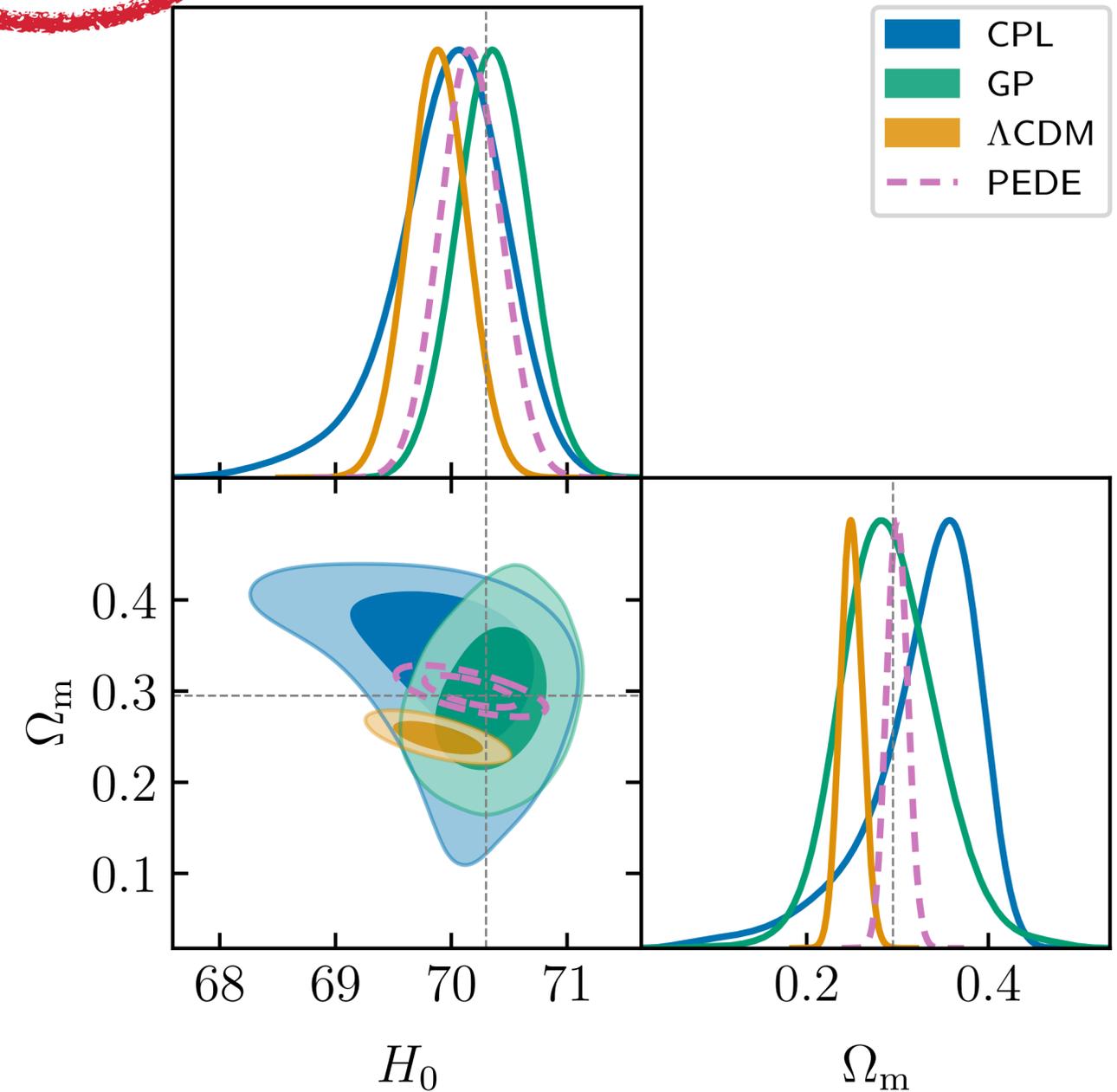
# Non-parametric approach

PEDE Universe | Pantheon+ & ET  $\Delta$  + CE

Phenomenologically Emergent Dark Energy



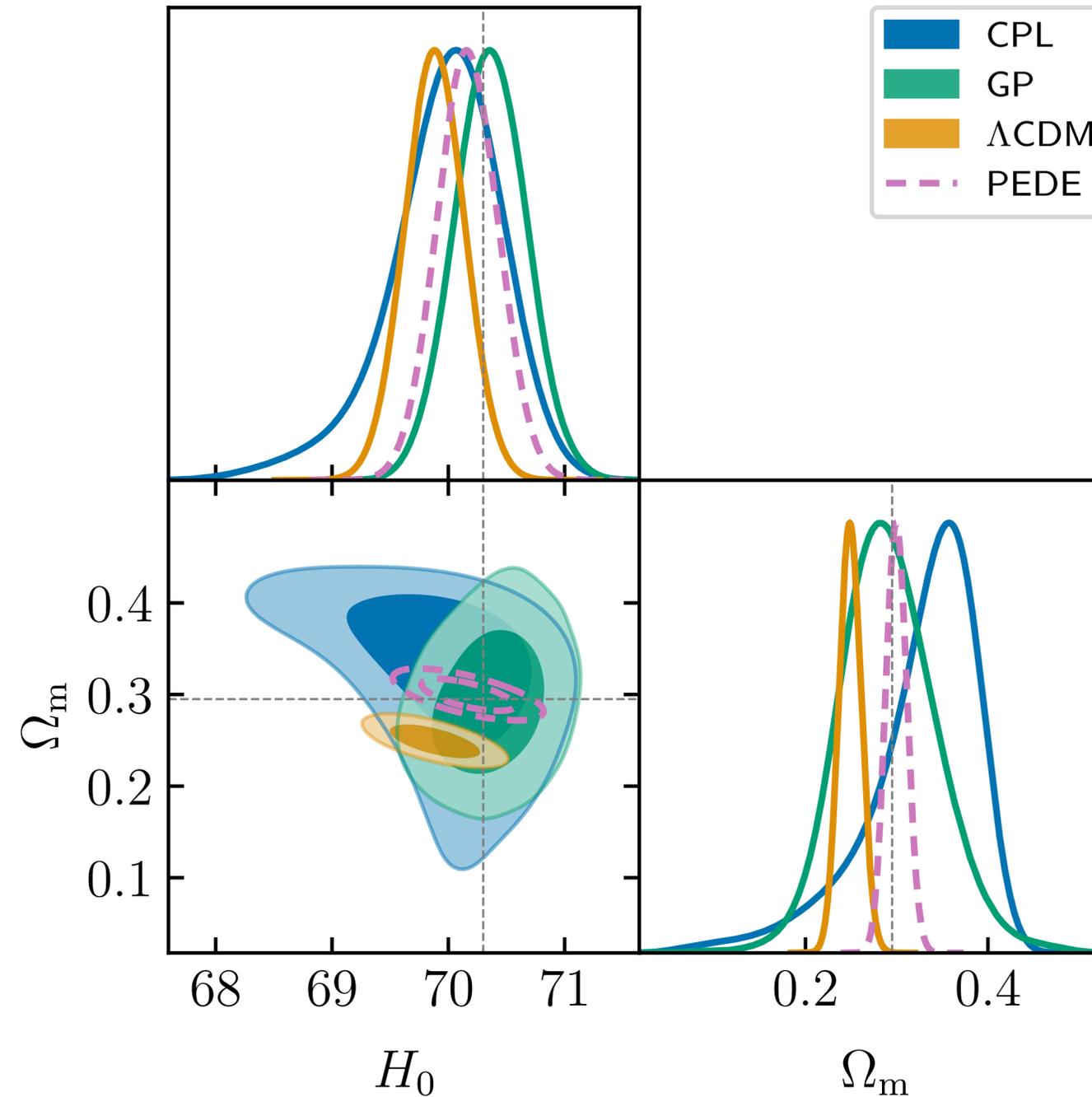
Li and Shafieloo, 2019



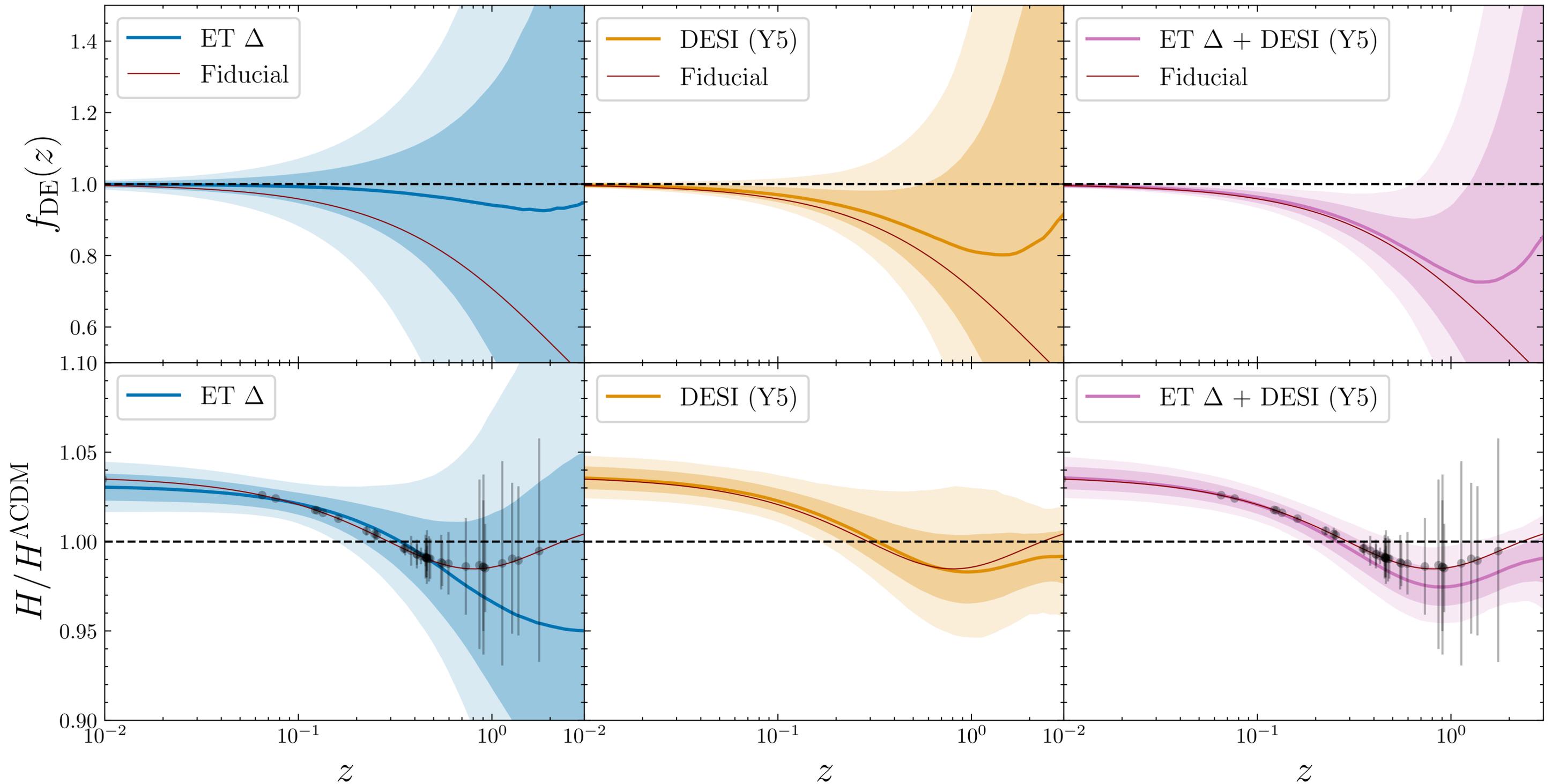
Cozzumbo+, 2024

# Non-parametric approach

PEDE Universe | Pantheon+ & ET  $\Delta$  + CE



# Non-parametric approach



# Two birds with one method

DDE

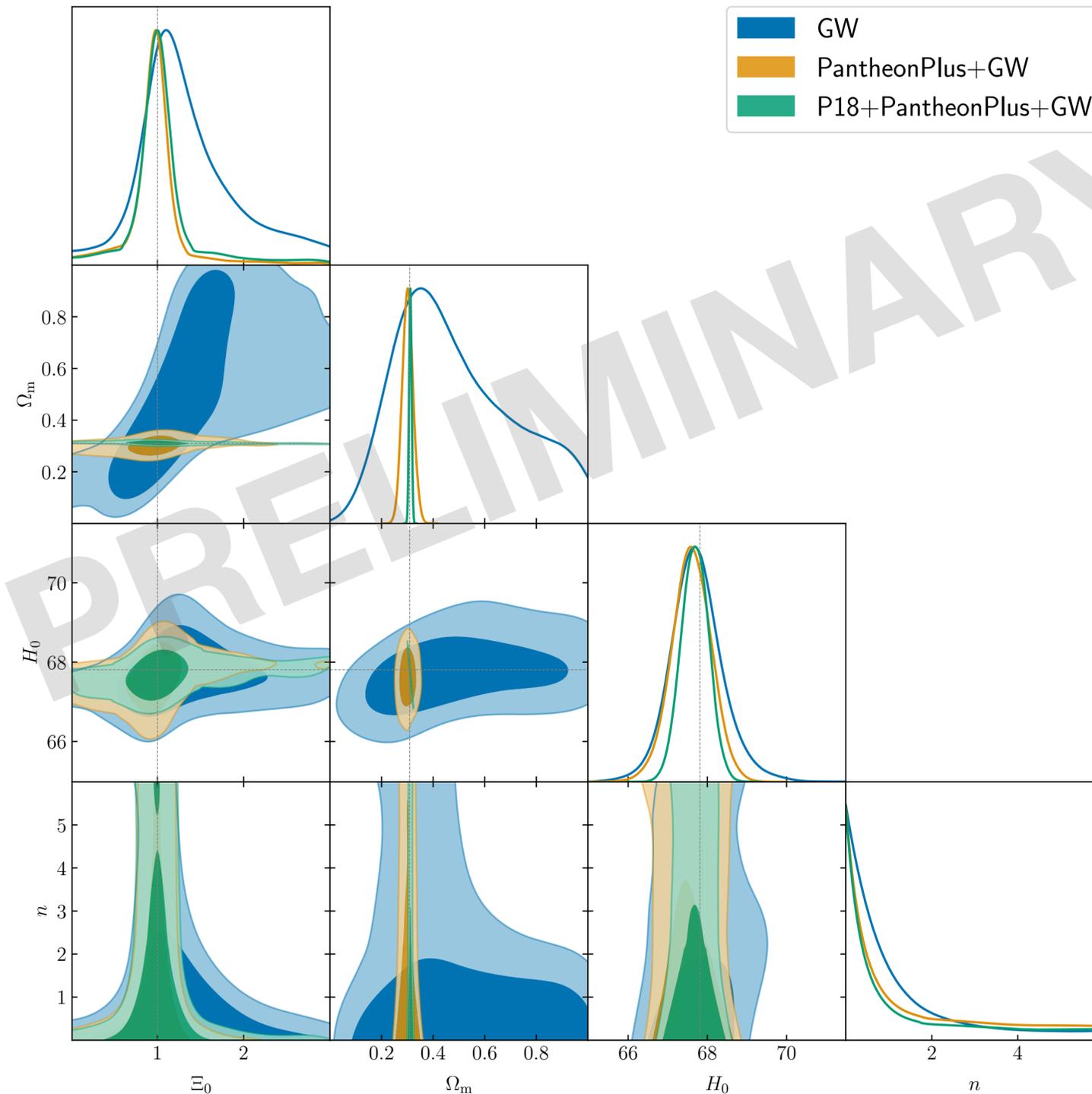
$$H(z) = H_0 \sqrt{\Omega_{m,0}(1+z)^3 + \Omega_{\text{DE},0} A(z)}$$

MG

$$\frac{d_L^{\text{GW}}(z)}{d_L^{\text{EM}}(z)} = \Xi_0 + \frac{1 - \Xi_0}{(1+z)^n} = B(z)$$

# Modified gravity

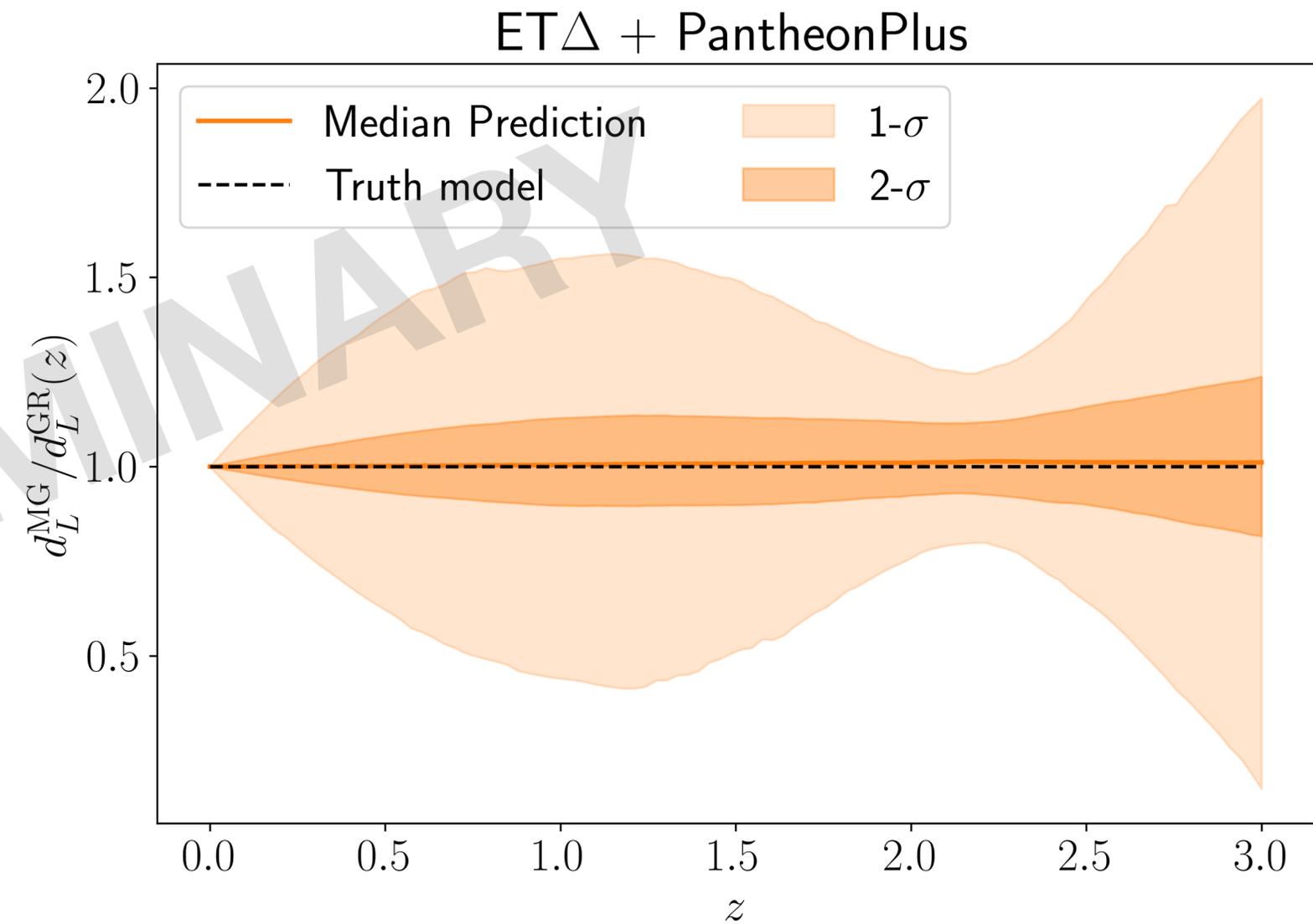
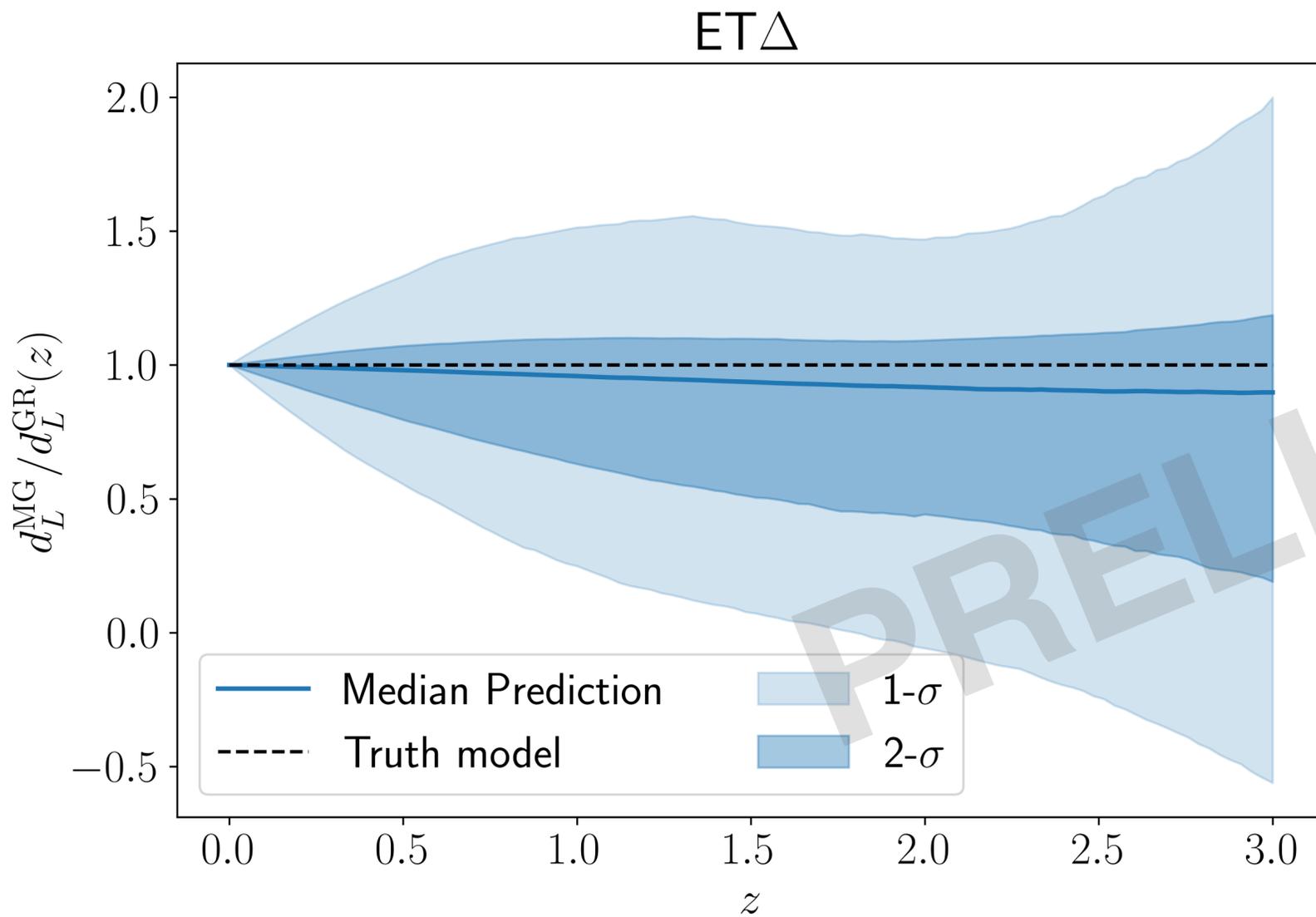
$\Lambda$ CDM Universe |  $ET\Delta$  | 38 ev



Cozzumbo+, in prep.



# Modified gravity



Cozzumbo+, in prep.



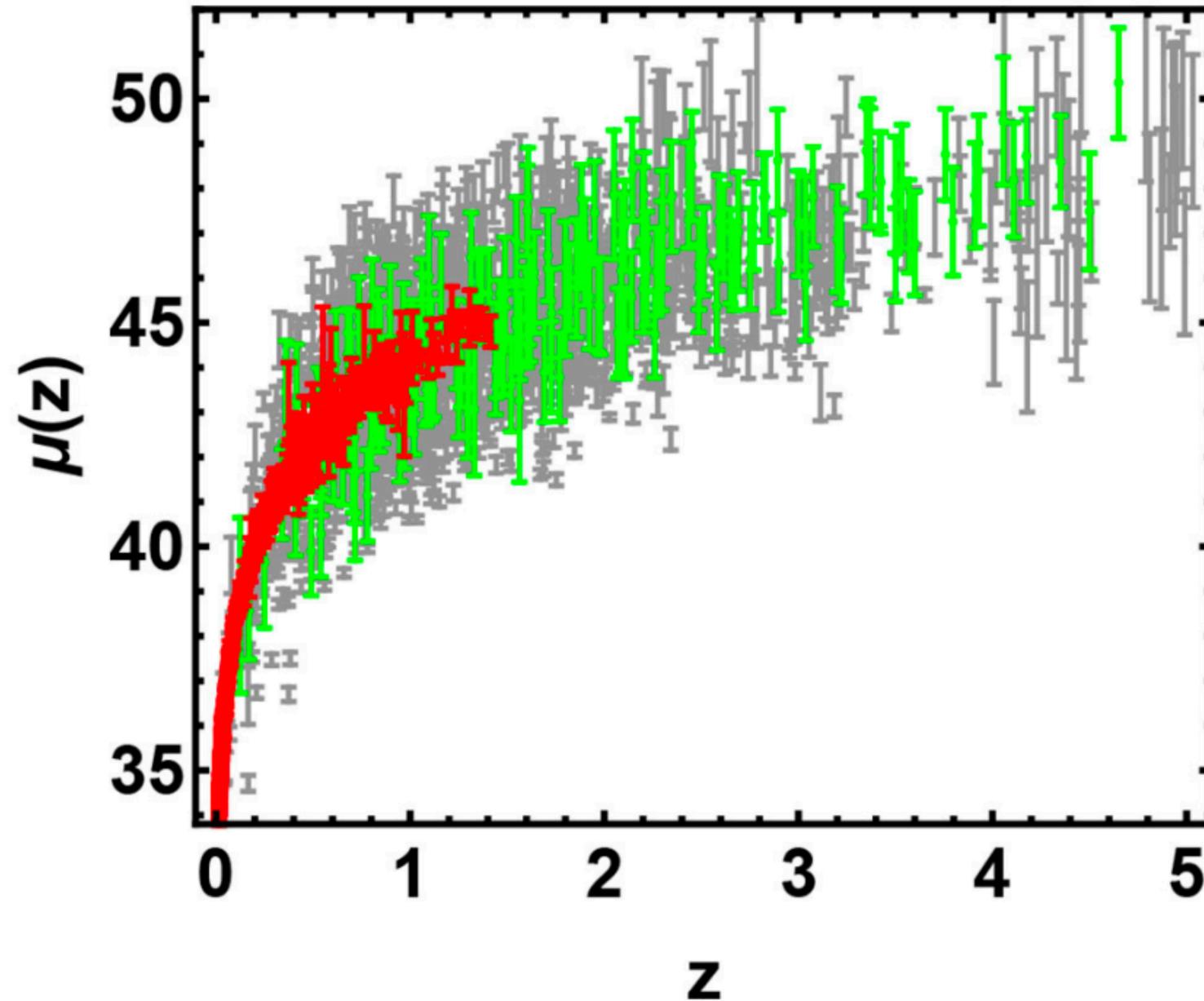
# Conclusions

- We compare different catalogs of GRBs and configuration of 3G GW detectors to understand the **future prospects of cosmological constraints with Bright Sirens**
- We compare parametric and non-parametric approaches, underlining the **biases incurring when choosing the wrong fitting model**.  
The non-parametric reconstruction is a factor  **$\sim 1.5$  better** than the parametric one.
- We show the potential of a model-independent reconstruction for **Einstein Telescope and next generation cosmological probes**.  
With less than **40 GRBs** we will be able to achieve unprecedented precision on  $H_0$  and  $\Omega_m$  and accurately reconstruct the **DE density evolution** and the **nature of gravity**.

# Backup

# Standard candles

Demianski+ 2020

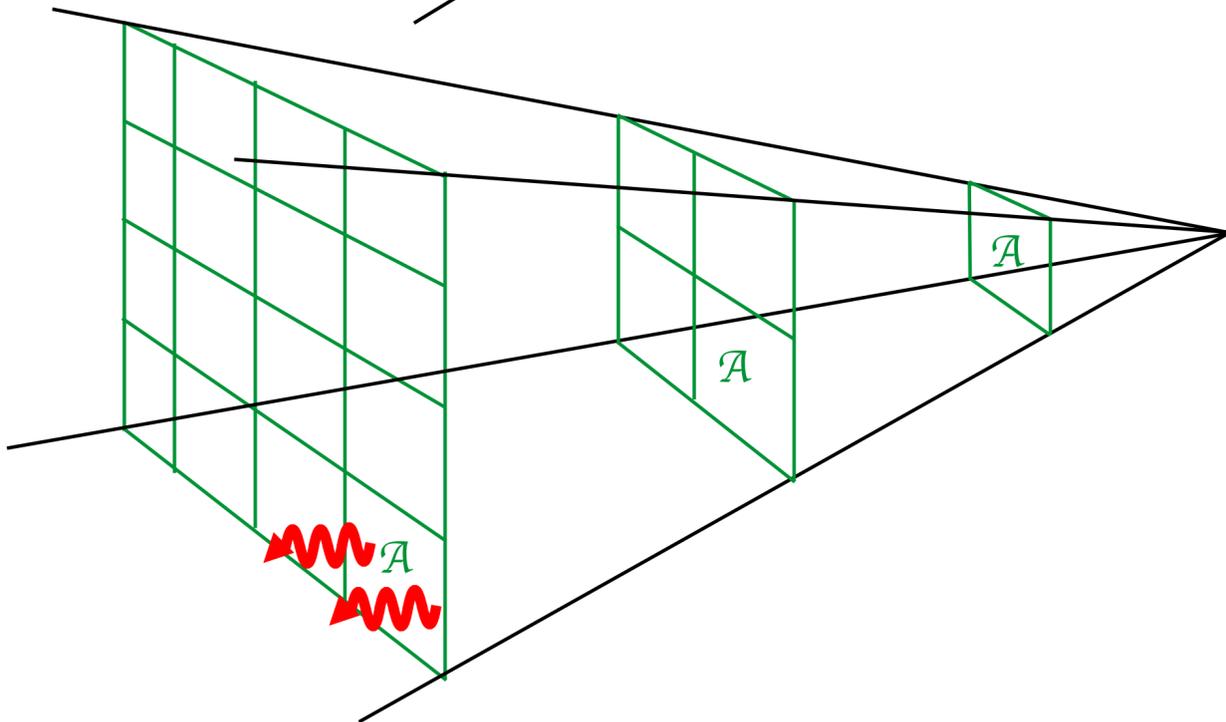
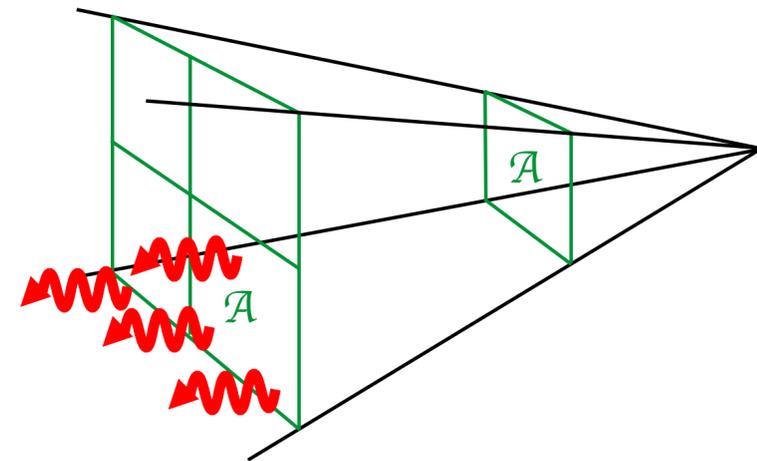
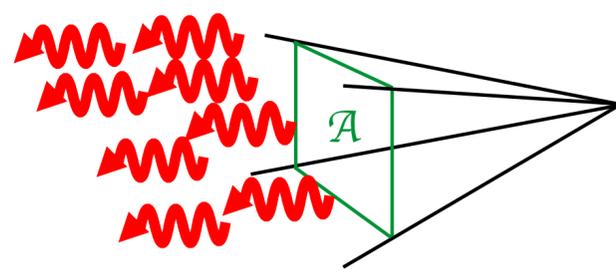


SN Ia (Cepheids)

GRBs (SN Ia)

QSOs ( $F_X - F_{UV}$ )

# Standard candles



Related to absolute magnitude ( $M$ )

$$d_L^2 = \frac{L}{4\pi F}$$

Measured

$$m - M = \mu = 5 \log_{10} \left( \frac{d_L}{1 \text{Mpc}} \right) + 25$$

# Modified gravity theories

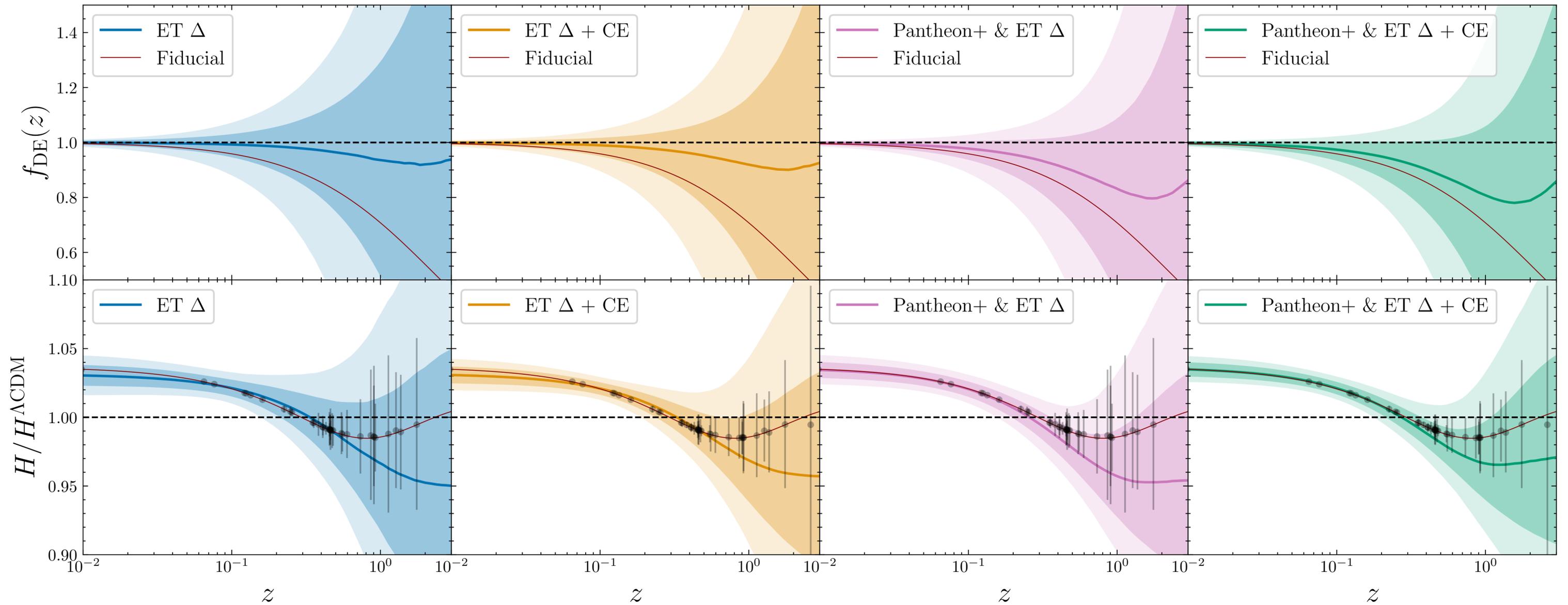
$$\tilde{h}_A'' + 2\mathcal{H} [1 - \delta(\eta)] \tilde{h}_A' + k^2 \tilde{h}_A = 0$$

$$\frac{\tilde{a}'}{\tilde{a}} = \mathcal{H} [1 - \delta(\eta)]$$

$$\tilde{h}_A \propto \frac{\tilde{a}(z)}{\tilde{a}(0)} \frac{a(0)}{a(z)} \frac{1}{d_L(z)} = \frac{\tilde{a}(z)}{a(z)} \frac{1}{d_L(z)} = \frac{1}{d_L^{\text{GW}}(z)}$$

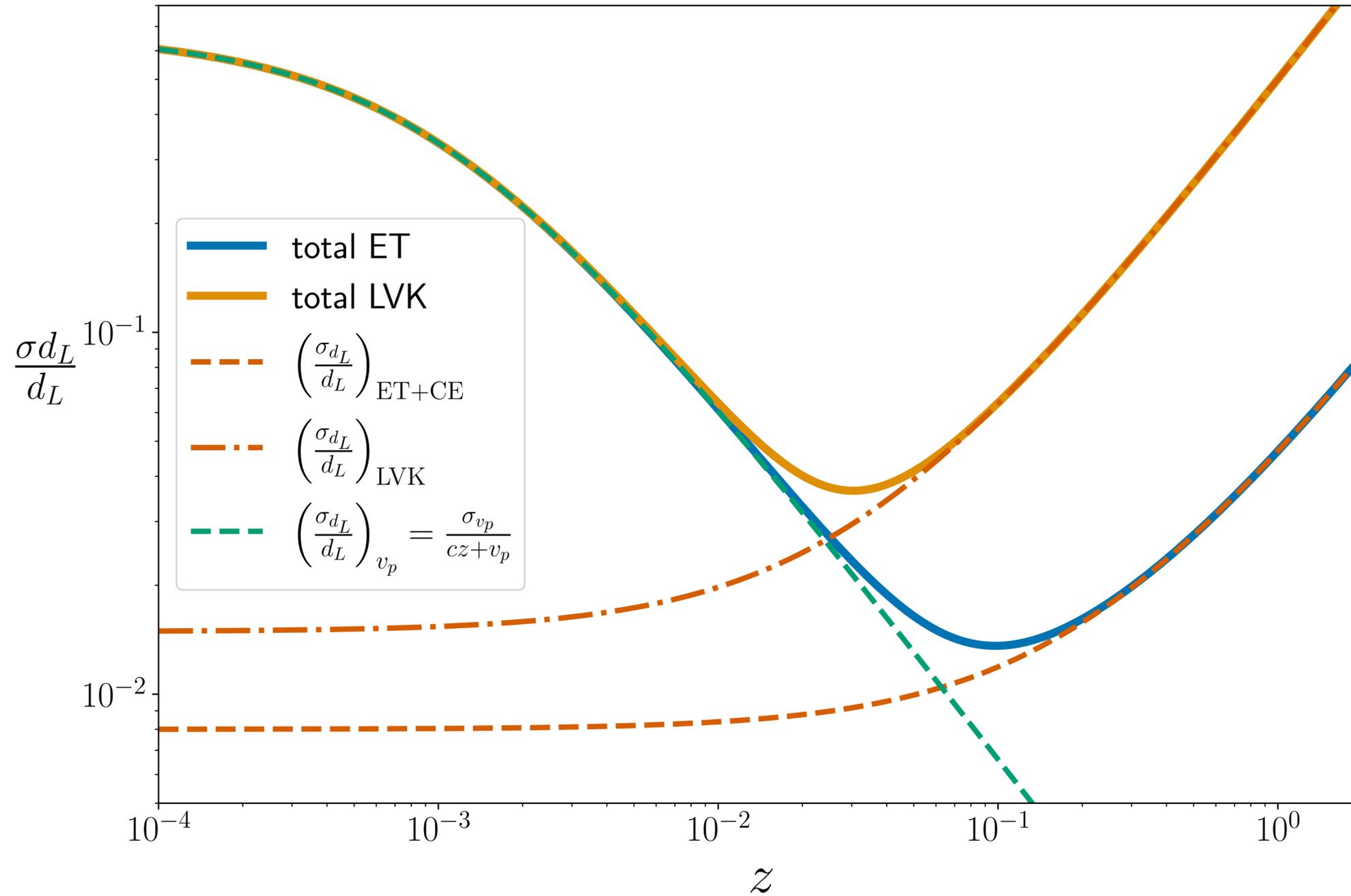
$$\frac{d_L^{\text{GW}}(z)}{d_L^{\text{EM}}(z)} = \Xi_0 + \frac{1 - \Xi_0}{(1+z)^n}$$

# Non-parametric approach

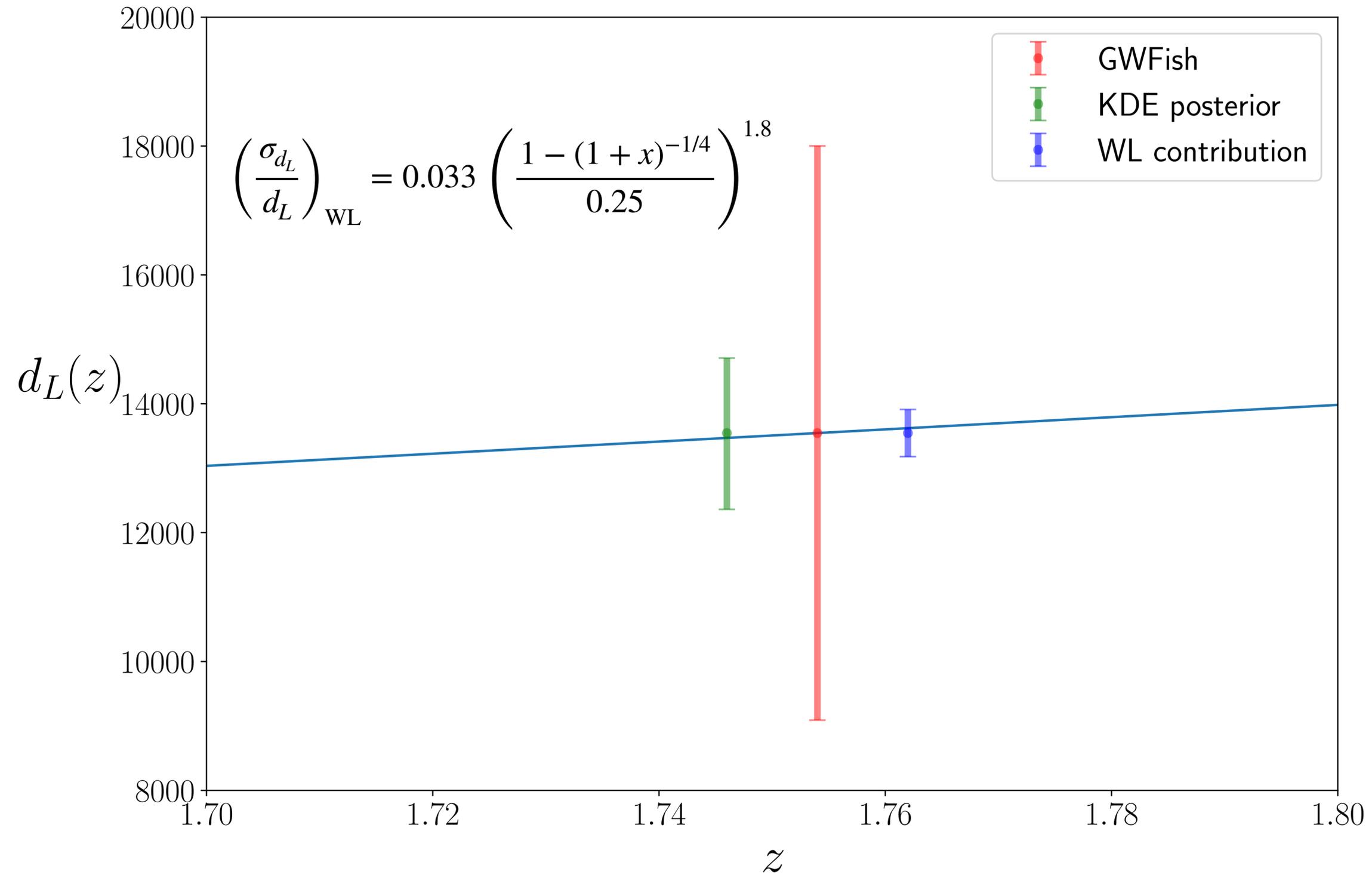


Cozzumbo+, 2024

# Systematics



# Systematics



# PEDE

$$f_{\text{DE}}(z) = 1 - \tanh(\log_{10}(1+z))$$

$$w(z)^{\text{PEDE}} = \frac{1}{3} \frac{d \ln f_{\text{DE}}(z)}{dz} - 1 = -\frac{1}{3 \ln 10} \left( 1 + \tanh(\log_{10}(1+z)) \right)$$